

Operations on Functions

Evaluating Functions

* this is just substitution

Ex 1 $h(a) = -a + 4$

Find $h(-1) = -(-1) + 4$

$$h(-1) = 1 + 4$$

$$h(-1) = 5$$

Try this!

$$k(a) = 3a + 4$$

Find $k(6)$

$$f(n) = 5^{-n} + 2$$

$$f(-2) = 5^{(-2)} + 2$$

$$f(-2) = 5^2 + 2$$

$$f(-2) = 25 + 2$$

$$f(-2) = 27$$

$$\begin{array}{l} \downarrow \quad \downarrow \\ x \quad \quad y \\ (-2, 27) \end{array}$$

$$f(x) = 2^x + 6$$

$$f(-1) = 2^{-1} + 6$$

$$f(-1) = \frac{1}{2} + \frac{12}{2}$$

$$f(-1) = \frac{1}{2} + \frac{12}{2}$$

$$f(-1) = \frac{13}{2}$$

Ex

$$f(x) = x^2 + 3 \quad g(x) = 3x - 10$$

find $(f+g)(x) = x^2 + 3 + 3x - 10$

$$(f+g)(x) = \underline{x^2 + 3x - 7}$$

$$\begin{aligned} \text{find } (f+g)(10) &= 10^2 + 3(10) - 7 \\ &= 100 + 30 - 7 \\ &= 130 - 7 \\ &= \underline{123} \end{aligned}$$

Subtraction

$$(f-g)(x) = f(x) - g(x)$$

* don't forget to distribute the neg.

Ex $f(x) = 2x - 9 \quad g(x) = 3x - 12$

$$(f-g)(x) = 2x - 9 - (3x - 12)$$

$$= 2x - 9 - 3x + 12$$

$$= \underline{-x + 3}$$

Multiplying

$$(f \cdot g)(x) = f(x) \cdot g(x)$$

often requires FOIL

Ex $f(x) = x - 4$ $g(x) = 5x - 7$

$$\begin{aligned} (f \cdot g)(x) &= (x - 4)(5x - 7) \\ &= 5x^2 - 7x - 20x + 28 \\ &= \boxed{5x^2 - 27x + 28} \end{aligned}$$

Division

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$$

Ex $f(x) = 4x + 5$ $g(x) = 4x - 7$

$$\left(\frac{f}{g}\right)(x) = \frac{4x + 5}{4x - 7}$$

$$\frac{3n+4}{3n}$$

$$\frac{2x+4}{2x}$$
$$\frac{2(x+2)}{2x}$$

$$|-x + 2|$$

$$1 - 11 \quad \text{odd}$$

$$13 - 21 \quad \text{odd}$$

$$33 - 41 \quad \text{odd}$$