

8.1 Multiplying and Dividing Rational Expressions Date _____ Period _____

Simplify each and state the excluded values.

1) Factor all numerators and denominators

2) Cancel any common factors

3) State the excluded values

* An excluded value is a number that makes the denominator = 0

* These come from the factored form of the denominator

EXAMPLES:

1) $\frac{n+5}{n^2-2n-35}$

Factor: $\frac{n+5}{n+5}$

cancel $\frac{(n-7)(n+5)}{n-7 \quad n+5}$
↓ ↓
 $n \neq 7 \quad n \neq -5$ ← excluded values

$$\frac{1}{n-7}; n \neq 7, -5$$

2) $\frac{x-4}{9x-36} = \frac{x-4}{9(x-4)}$
↓
 $x \neq 4$

$$\frac{1}{9}; x \neq 4$$

3) $\frac{1}{8x-72} \cdot \frac{8x-72}{7x}$

$$\begin{aligned} 8x-72 &= 0 & 7x &= 0 \\ 8x &= 72 & x &= 0 \\ x &\neq 9 & & \end{aligned}$$

$$\frac{1}{7x}; x \neq 0, 9$$

4) $\frac{1}{x+9} \cdot \frac{x^2+6x-27}{6x+42}$

$$\frac{1}{x+9} \cdot \frac{(x+9)(x-3)}{6(x+7)}$$

↓ ↓
 $x \neq -9 \quad x \neq -7$

$$\frac{(x-3)}{6(x+7)}; x \neq -9, -7$$

$$5) \frac{\frac{1}{a+1} \cdot \frac{a^2+a-72}{a-8}}{a^2+a-72}$$

we do not \div by fractions, we multiply by the reciprocal

$$\frac{1}{a+1} \cdot \frac{a^2+a-72}{a-8}$$

$$\frac{1}{(a+1)} \cdot \frac{(a+9)(\cancel{a-8})}{(\cancel{a-8})}$$

\downarrow $a \neq -1$ \downarrow $a \neq 8$

$$\boxed{\frac{a+9}{a+1}; a \neq -9, -1, 8}$$

$$6) \frac{v^2-11v+10}{8} \div \frac{v^2-18v+80}{v-8}$$

$$\frac{v^2-11v+10}{8} \cdot \frac{v-8}{v^2-18v+80}$$

$$\frac{(v-10)(\cancel{v+1})}{8} \cdot \frac{\cancel{v-8}}{(v-10)(\cancel{v-8})}$$

\downarrow $v \neq 10$ \downarrow $v \neq 8$

$$\boxed{\frac{v+1}{8}; v \neq 8, 10}$$

* for division problems

* excluded values come from the denominator of the first fraction and the numerator and denominator of the fraction you are dividing by.